

Anharmonicity in the non-rotational region of rare earths

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For the non-deformed nuclei ($2.05 < R_{4/2} < 3.0$), a plot of $E(4_1)$ versus $E(2_1)$ yields a linear relation with a slope of 2.0 [1]. For the varying energy E_2 , the intercept ϵ_4 is constant (Fig. 1). This can be expressed as

$$E_4 = 2 E_2 + \epsilon_4, \quad (1)$$

A constant ϵ_4 was ascribed to a constant anharmonicity. In terms of the anharmonic model expression [2]

$$E_I = a I + bI(I-2) \quad (2)$$

ϵ_4 is $8b$. In the absence of a cubic term, denoting rotation vibration interaction, ‘a’ and ‘b’ stay constant for all I in a given nucleus. Also, $\epsilon_4 = E_{\gamma(2)} - E_{\gamma(1)} = \Delta E_{\gamma}$, which is related to dynamic moment of inertia $J^{(2)} = 4/\Delta E_{\gamma}$ according to rotation model. So ϵ_4 is inverse dynamic moment of inertia in RM. We study

constancy of ϵ_4 (or b or $J^{(2)}$) with E_2 . Rewrite Eq. 1 as

$$R_4 = 2.0 + \epsilon_4/E(2_1). \quad (3)$$

a) If one assumes a constant $\epsilon_4 = 160$ keV, for $E_2 = 160$ keV, E_4 would be $320 + 160 = 480$, so that Eq. (2) yields $R_{4/2} = 3.0$.

b) For $E_2 = 800$ keV, it yields $R_{4/2} = 2.2$.

Thus a constant value of residual energy ϵ_4 is in principle possible for the whole region of $E_2 = 160-800$ keV. The variation of $R_{4/2}$ and E_4 is absorbed in E_2 . A varying $R_{4/2}$ can yield constant ϵ_4 . But the arithmetic for the deformed region is different [1, 2]. At $E_2 = 70$ keV, $R_{4/2} = 10/3$ and ϵ_4 should be about 90 keV only. Just below the deformed region, defined by $R_{4/2} > 3.0$ and $E_2 = 120-130$ keV, ϵ_4 would be 120-130 keV. This sets the lower limit on the deformed side, ϵ_4 varying 90-130 keV.

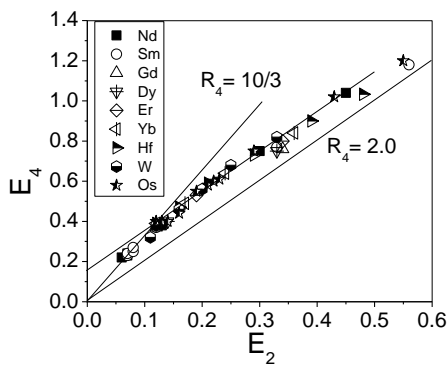


Fig. 1. Plot of E_4 versus E_2 . Lines from the origin have slope of 2 and 10/3.

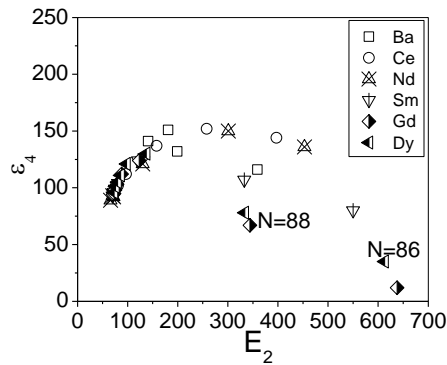


Fig. 2. Plot of residual energy ϵ_4 for Q-I.

Real nuclei

A mean value of $\epsilon_4=(160 \pm 50)$ keV is indicated for the whole range of E_2 from about 120-700 keV. For a search of the systematics of ϵ_4 we study the data quadrant wise. In Quad-I ($N<104, Z=54-66$) (Fig. 2), for $N=86$ ($E_2\sim 600$ keV) data of Sm, Gd and Dy, the value of ϵ_4 is very low, off the general trend on the right. In the middle, also $N= 88$ data of $Z=62, 64, 66$ ($E_2=300$ keV) lie off downwards. Next, on the

deformed side (on the left) also ϵ_4 falls below 125, reflecting saturation effect. Excluding these data, others lie at about 125-150 keV In Quadrant-II ($N<104, Dy-Pt$)(Fig. 3) again ϵ_4 is below 125 keV on deformed side, ($E_2 <150$ keV). Next Pt data on left are also off, ($E_2 <250$ keV). Six data on right, of Dy, Er, Yb, Hf also lie low below 100 keV (non-collective effect). Data on smooth curve lie at 140 to 175 keV

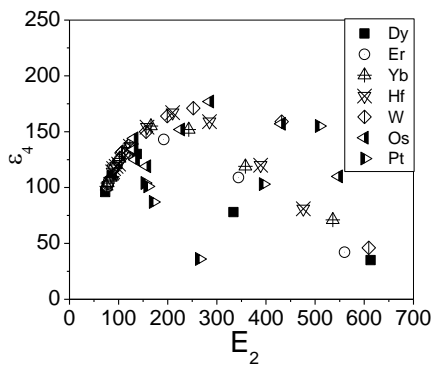


Fig. 3. Plot of residual energy ϵ_4 Quad. II.

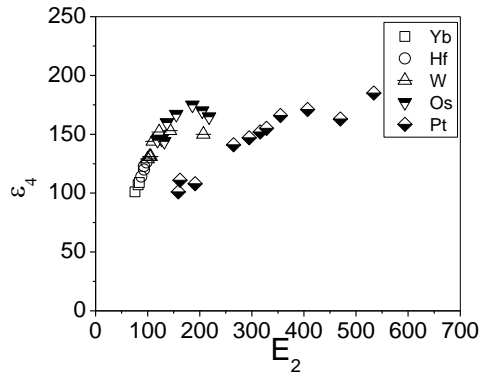


Fig. 4. Plot of residual energy ϵ_4 Quad. III.

In Quadrant-III ($N>104, Yb-Pt$)(Fig. 4), excluding data of deformed nuclei ($E_2<130$ keV), and 3 other points, ϵ_4 lies at 125-175 keV. This study illustrates how the residual energy varies with N, Z quadrant wise

Discussion

A constant gradient= $\Delta E_4/\Delta E_2$ holds good approximately for non-deformed region, in spite of the varying structure. But in Eq. (1), a constant intercept has differing effect on nuclei of different E_2 . The Eq. (1) also holds good for higher spin I, with slope of (I/2), which implies the application of phonon rule in the spectrum of all non-deformed nuclei, before the phase transition, from anharmonic to deformed, at X(5) symmetry point [4]. The differing range of ϵ_4 in different quadrants arises on account of the fact that for same E_2 energy, E_4 is different, reflecting the different underlying microscopic structure.

The anharmonicity represents either a symmetric change in the width of a harmonic oscillator potential well due to the quadratic term, or the asymmetry of the well due to the cubic term. This is not constant with varying R_4 . Moreover, the split in the 2 phonon triplet states varies continuously. Other attributes of structure vary with E_2 . *It highlights the fact that the near constancy of ϵ_4 is related to the rotational invariance of the angular momentum projected states in the ground state band from an intrinsic state, and not to the vibrational states.*

Reference

[1] R. F. Casten et al, Phys. Rev. Lett. **71**, 227 (1993).
 [2] T.K. Das et al. Phys. Rec. C2, 632 (1970)
 [3] R. V. Jolos et al., Phys. Rev. **C54**, R2146 (1994).
 [4] F. Iachello, Phys. Rev. Lett. 87, 2502 (2001).