

Correlation of β -band with ground state band in medium mass nuclei

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The low energy levels of even Z even N nuclei in medium mass region $A = 150 - 200$ away from closed shells develop collective characteristics. The lowest levels can be grouped into three K - bands. The lowest one based on the ground state forms the ground state rotational band. The rotational band, based on the axially symmetric vibration of the nuclear core with $K=0_2$ is called the beta vibrational band. The one based on the axially asymmetric vibration of the nuclear core with $K = 2$ projection on the symmetry axis is called the $K = 2, \gamma$ - vibrational band. There is interest in the nature of the $K=0_2$ band. This is called the geometric view of the Bohr Mottelson unified collective model [1]. In the algebraic Interacting Boson model [2], the $K=0_2$ and $K=2$ bands belong to the $(2N-4, 2)$ family of states. In IBM, strong β - γ E2 transitions comparable to γ -g are predicted. This led to a possibility of interpreting the $K=0_2$ band as $\gamma\gamma$ vibration [3]. Whether, this is applicable to all nuclei or to only a few special ones led to an extensive study of the

characteristics of the $K=0_2$ bands [4,5]. The problem seems to be still unresolved. In the present work, we study the nature of the $K=0_2$ bands by studying the correlations of some collective observable of the $K=0_2$ band and the ground state band.

If the quadrupole deformation of the nuclear core is unchanged in the intrinsic $K=0_2$ vibrations, then the energy separation $E(2_\beta) - E(0_\beta)$ should be same as $E(2_g)$. So we plot the former against the latter in Figure 1, for the Sm-Hf nuclei with $N < 104$. The $N = 88$ isotones of Sm, Gd, Dy, Er lie at the right top corner. At $N=90$, there is a sharp drop in $E(2_g)$ energy. The same is true for $K=0_2$ band. This drop increases progressively with decreasing Z , for Er to Sm. (see the data at about 150 keV). For $N > 90$, the data lie condensed within a short span of 80 - 120 keV on account of saturation phenomenon of the deformation effect of the valence nucleons. However, the $E(2_\beta) - E(0_\beta)$ remain almost equal to $E(2_g)$.

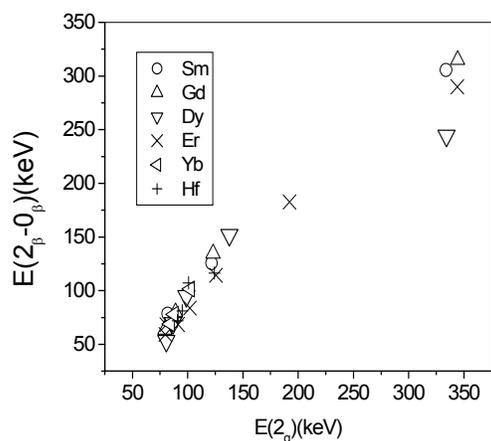


Fig. 1: The energy difference of $E(2_\beta)/E(0_\beta)$ versus $E(2_g)$.

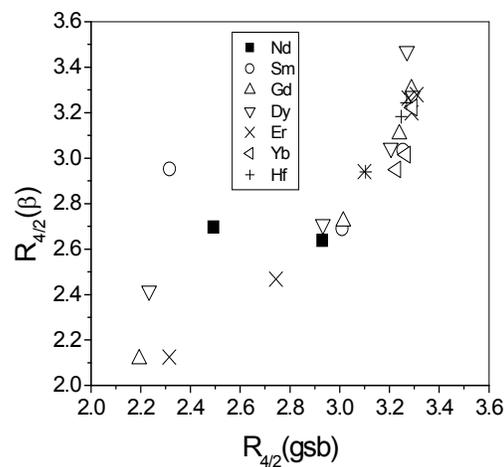


Fig. 2: $R_{4/2}(\beta\text{-band})$ vs. $R_{4/2}(\text{ground band})$.

The energy ratio $R_{4/2} = E(4)/E(2)$ is a good measure of the deformation of a nucleus. With the variation in N, Z it can assume a value of 2.0 for the spherical vibrator to 3.33 for the deformed rotor. For a collective rotation based on the intrinsic axial vibration the value of $R_{4/2}$ is expected to be the same for the $K = 0_2$ band and the ground state band. In Fig. 2, $R_{4/2}$ for $K = 0_2$ band is plotted against $R_{4/2}$ of ground band for the nuclei of Nd - Hf, $N < 104$. Except for ^{150}Sm ($R_{4/2} = 2.32$) and ^{148}Nd (filled square), all other data form a single smooth curve, indicating a close

relationship of the two bands for all nuclei in the spherical to deformed region.

To further explore this relationship, we obtained the ratio r of $R_{4/2}$ for the $K = 0_2$ band and the ground band and plot it versus neutron number N (Fig. 3). If these are equal, the ratio should be one. In Fig. 3, most points lie below $r = 1.0$. There is a pattern of the deviation from ideal value of 1.0, versus N and Z. Most points lie within $r = 0.9 - 1.0$, except $N = 88$ Sm and Dy. To within 10% deviation, the two bands are correlated. This smaller $R_{4/2}(\beta)$ provides a challenge for nuclear theory.

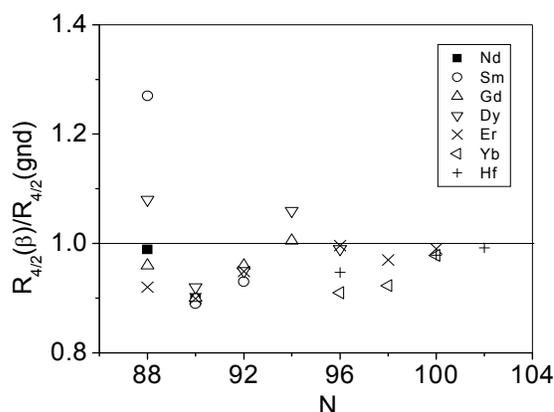


Fig 3: Variation of $R_{4/2}(\beta\text{-band}) / (R_{4/2} \text{ ground})$ with N.

Conclusion:

A close correlation of the collective characteristics of the $K=0_2$ β - band and ground band in $A=150-200$ region of Nd- Hf is demonstrated.

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