

# Scaling Behaviour of the Multiplicity Distribution of Shower Particles at 3.7 A GeV

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## Introduction

The use of nuclear emulsion both as a target and a detector can be used to study the properties of charged secondary particles.

The aim of present work is to investigate the validity of well-established KNO type scaling behavior of multiplicity distribution of shower particles produced in <sup>28</sup>Si-emulsion at 3.7 A GeV interactions with different emulsion target groups. The number of interacting projectile protons and multiplicity characteristics of different charged secondary particles can be determined accurately for each collision event. Various other useful consequences of multiparticle production such as variation of the ratio of  $D/\langle n_s \rangle$  as a function of  $n_g$  at 3.7 A GeV energy have also been analyzed.

## Experimental Details

In the present experiment stacks of NIKFI BR2 nuclear emulsion of dimension 16.9 x 9.6 x 0.06 cm<sup>3</sup> have been exposed horizontally to a <sup>28</sup>Si beam of 3.7 A GeV per nucleon at JINR Dubna. Each primary <sup>28</sup>Si track has been followed using along the track scanning technique on an OLYMPUS BH2 microscope under a magnification of 2250 in order to search for inelastic collision events. Classification of different charged secondaries can be seen from our previous publications [1].

## Results

### KNO Scaling

According to this law, at the asymptotic energies, the probability  $P(n)$  to produce  $n$  charged particles in the final state is related to a scaling function  $(n/\langle n \rangle)$  according to the following relation:

$$\langle n \rangle P(n) = (n/\langle n \rangle) \quad (1)$$

This behavior of multiplicity distribution as a function of variable  $z'$  is referred as KNO scaling [2] and given as

$$P(n_s) = \sigma_n/\sigma_{inel} = 1/\langle n_s \rangle (z') \quad (2)$$

KNO behavior is independent of energy of incident hadron and atomic mass of  $A_T$  of target nucleus,  $\sigma_n$  denotes the partial cross section of producing  $n$  charged particles and  $\sigma_{inel}$  denotes the total inelastic cross section.

Fig. 1 (a), (b) & (c) we plot  $(z')$  vs  $z'$  for <sup>28</sup>Si interaction with emulsion at 3.7 A GeV for H-events, CNO-events and AgBr-events respectively. From this figure we can see that the KNO scaling behavior of multiplicity distributions is well satisfied by shower particles produced in <sup>28</sup>Si-emulsion interactions with different emulsion targets (H, CNO & AgBr) at 3.7 A GeV. In Table 1, we present the experimental values of Dispersion  $D = [\langle n_s \rangle^2 - \langle n_s^2 \rangle]^2$  of shower particles in <sup>28</sup>Si-emulsion interactions. A consistent trend is seen in the data using different projectile. The ratio  $\langle n_s \rangle / D$  for hadron-nucleus and nucleus-nucleus collision is similar, indicating essential similarity in the production mechanism of two types of collision. In case of nucleus-nucleus collision,  $D$  increases as the mass number of projectile increases.

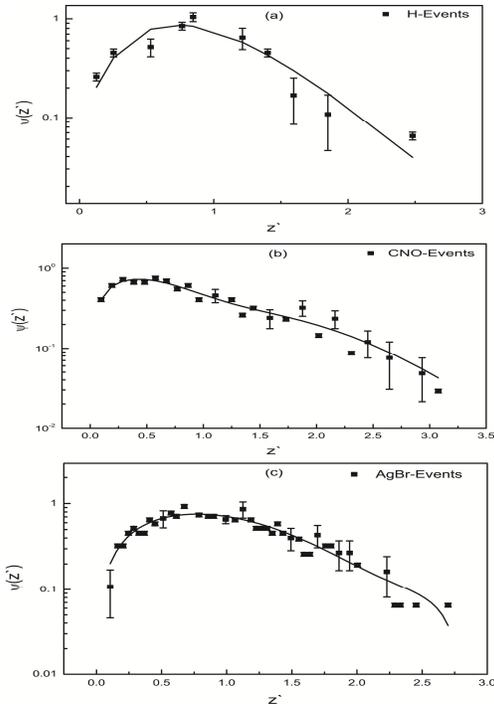
**Table 1:** Variation of  $\langle n_s \rangle$ , dispersion  $D$  and  $\langle n_s \rangle / D$  as a function different emulsion target groups.

Interaction	$\langle n_s \rangle$	$D$	$\langle n_s \rangle / D$
<sup>28</sup> Si- CNO	10.40±0.54	6.030.32	1.72±0.15
<sup>28</sup> Si -AgBr	24.44±1.26	13.850.71	1.76±0.18
<sup>28</sup> Si-em	15.32±0.22	10.080.22	1.52±0.02

### Number of Interacting Nucleons

The number projectile nucleons interacting with target ( $N_{int}$ ) is one of the basic parameter of superposition model [2], in which we consider that the nucleons from the incoming nucleus

interact independently of one another i.e. a nucleus-nucleus (A-A) collision is a superposition of nucleon-nucleus (N-A)



**Fig.1** Variation of  $\psi(z')$  as a function of  $z'$  for H-Events (a), CNO-Events (b) and AgBr-Events (c).

collisions[3]. The number of interacting nucleons is determined by the relation

$$\langle N_{int} \rangle = A - (A/Z) Q = A - 2Q \quad (3)$$

Where A and Z are the mass and charge of number respectively of projectile nucleus and Q is the average total charge of projectile spectator fragments (non-interacting PFs) which can be determined on event by event basis as

$$Q = \sum n_i Z_i \quad (4)$$

Where  $n_i$  is the number of projectile fragments with charge  $Z_i$  and summation is made to include all fragments. Using relation (3) and (4), the average number of interacting nucleons is estimated to be  $\sim (13.74 \pm 0.45)$ . The average number of interacting nucleons of projectile can also be calculated by

$$\langle N_{int} \rangle = 0.73A^{0.72} \quad (5)$$

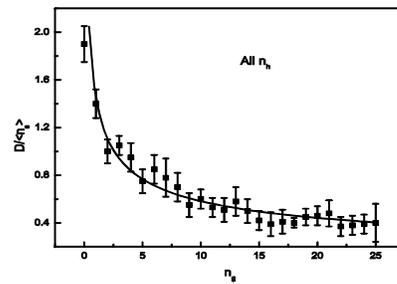
The experimental value of  $\langle N_{int} \rangle$  using (3) is higher than that of phenomenological value (8.04). This may be due to angular restriction

imposed ( $\leq 5^\circ$ ) in defining the  $Z \geq 2$  projectile fragments. The average number of interacting nucleons of projectile determined by equation (3), for colliding with targets (i.e. H, CNO and AgBr) is found to be  $(6.86 \pm 0.51)$ ,  $(12.38 \pm 0.77)$  and  $(17.82 \pm 0.81)$  respectively.

Fig. 2 shows the dependence of  $D/\langle n_s \rangle$  as a function of  $n_g$ . We can see that the variation of  $D/\langle n_s \rangle$  with  $n_g$  follows the relation

$$D/\langle n_s \rangle = c(n_g)^d, \quad (6)$$

Where  $c = 1.75 \pm 0.06$  and  $d = -0.55 \pm 0.02$  for the present data.



**Fig. 2** Variation of  $D/\langle n_s \rangle$  as a function of grey particles ( $n_g$ ) in  $^{28}\text{Si}$ -emulsion interactions at 3.7 A GeV.

From Figure, we can observe that the ratio  $D/\langle n_s \rangle$  decreases with increasing value of  $n_g$  according to the relation given by equation (6). This decrease in the value of  $D/\langle n_s \rangle$  is in contradiction with the collective tube according to which  $D/\langle n_s \rangle$  should remain constant with  $n_g$  and it favours model which include repeated collisions [3].

### Conclusion

The KNO type scaling behavior of the multiplicity distribution is well satisfied by shower particles produced in  $^{28}\text{Si}$ -emulsion interactions at 3 A GeV for CNO and AgBr events.  $D/\langle n_s \rangle$  decreases with increasing value of  $n_g$  as predicted by the theoretical equation.

### References

- [1] B. K. Singh et al., Nucl. Phys. **A 570** 819 (1994).
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