

Systematic dependence of asymmetric parameter in light and medium mass region

Reetu Kaushik¹ and S. Sharma*

¹Research Scholar, Department of Physics, Mewar University, Gangrar, Rajasthan-312901, India
Panchwati Institute of Engineering and Technology (Uttar Pradesh Technical University),
National Highway- 58, Ghat Institutional Area, Meerut, PIN 250005, INDIA

*email: ss110096@gmail.com

Introduction

The study of collective nuclear structure with N , Z , N_B and $N_p N_n$ provide a detailed information of nuclear interactions involved. Several studies have been carried out to study the collectivity, deformation and systematic dependence of other nuclear properties on $N_p N_n$. de-Shalit & Goldhaber [1] pointed out the important role of valence nucleons. Talmi [2] noted the constancy of nuclear level structure in semi-magic isotones/isotopes. Hamamoto [3] observed that the p^+ & n^0 both are required for producing deformation. In IBM-1[4], the structure of nuclei depends on the total boson numbers N_B . The concept of F-spin multiplets was based on this and was well explained by Brentano et al. [5]. Casten [6] noted that the E_{2g^+} have smooth dependence on $N_p N_n$. Various studies [7] have been carried out to study the collectivity, deformation and systematic dependence of various nuclear observables on the product $N_p N_n$.

Gupta [8] observed that $1/\alpha$ was linearly dependent on $N_p N_n$, where the coefficient α contributes for rotational part of energy in the SU(3) symmetry limit of IBM[4] as,

$$E([N](\lambda, \mu) \text{ KLM}) = \alpha L(L+1) + \beta C(\lambda, \mu)$$

The $B(E2; 2_1^+ \rightarrow 0_1^+)$ values were also related with $N_p N_n$. Gupta et al. [9] noted a systematic dependence of γ -g B(E2) ratios on the $N_p N_n$ in different parts of the major shell space $Z=50-82$, $N<82$ and $N=82-126$. Casten and Zamfir [6] presented a review on the evolution of nuclear structure based on $N_p N_n$ product. The $N_p N_n$ scheme was further modified to use P- factor [9].

In this paper, we study the role of valence nucleons and holes on the nuclear structure, through $N_p N_n$. Casten and Zamfir [7] covered the various regions, viz., $A=100, 130, 150$ ($Z<64$, $Z>64$) and $A=190$. We present our results for $50 \leq Z \leq 82$ and $82 \leq N \leq 126$ region on *quadrant wise basis*.

The values of asymmetry parameter (γ) have been calculated for $50 \leq Z \leq 82$ and $82 \leq N \leq 126$ region and the whole data is divided into four quadrants and it has been plotted with $N_p N_n$ to study its systematics dependence.

Calculation of Asymmetric Parameter

The value of γ can be evaluated using the experimental energies $E_{2_2^+}$ and $E_{2_1^+}$ states [10]. The energy ratio $R\gamma = E_{2_2^+} / E_{2_1^+}$ and γ is:

$$\gamma = (1/3) \sin^{-1} [(9/8) \{1 - ((R\gamma - 1)/(R\gamma + 1))^2\}]$$

It can be evaluated using: (a) The energy ratio $R_4 = (E_{4g}/E_{2g})$ but only the nuclei with $2.8 \leq R_4 \leq 3.33$ will be allowed [11, 12]. (b) The B(E2) values which are very small and available with uncertainties. Therefore the values from energy ratio $R\gamma$ are more reliable.

Result and discussions

The variation of γ versus $N_p N_n$ product for quadrant-I for $50 \leq Z \leq 66$ and $82 \leq N \leq 104$ has been shown in Fig. 1. There is smooth dependence of γ with $N_p N_n$. The γ decreases from a maximum value of 30° for $N_p N_n = 0$ (i.e. SU(5) limit of IBM) to a minimum values of about 9° (i.e. SU(3) limit of IBM). The γ saturates for $N_p N_n \geq 30$. This shows non-dependence of γ with $N_p N_n$

because for a fixed value of $N_p N_n$ the γ is having varying values.

The variation of γ versus $N_p N_n$ for quadrant-II for $66 \leq Z \leq 82$ and $82 \leq N \leq 104$ has been shown in Fig. 2. There is smooth dependence of γ with $N_p N_n$ except Yb for $N_p N_n > 50$ and few Pt isotopes.

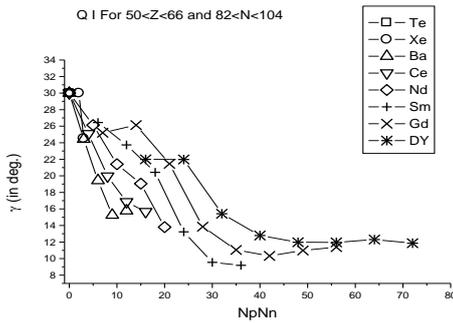


Fig.1 The variation of asymmetric parameter (γ) versus $N_p N_n$.

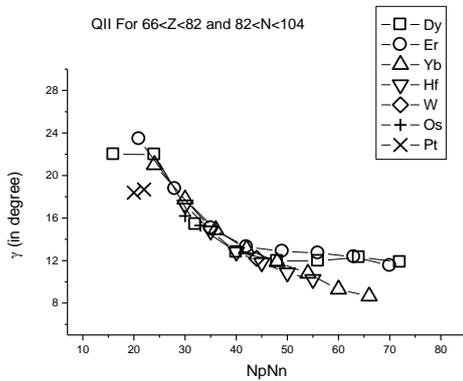


Fig. 2 The variation of asymmetric parameter (γ) versus $N_p N_n$ product for quadrant-II.

The variation of γ versus $N_p N_n$ for quadrant-III for $66 \leq Z \leq 82$ and $104 \leq N \leq 126$ has been shown in Fig. 3. There is smooth dependence of γ with $N_p N_n$ except Hg isotopes.

The graphs of γ against $N_p N_n$ vividly displays the formation of isotonic multiplets in quadrant-I, strong dependence on $N_p N_n$ in quadrant-II and weak constancy with Z in

quadrant-III is illustrated and support the findings of Gupta [13].

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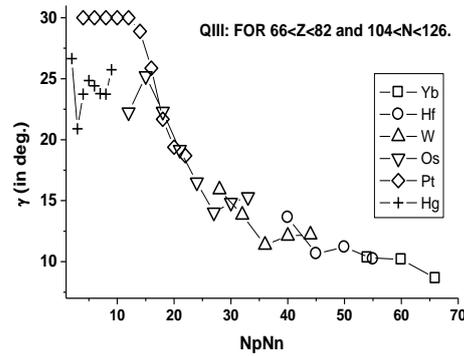


Fig. 3 The variation of asymmetric parameter (γ) versus $N_p N_n$ product for quadrant-III.

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