

# Alpha decay chains of superheavy nuclei

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## Introduction

A scientific knowledge on the nuclear stability in the superheavy mass region is a long-standing question. Hence, considerable attention has been given by the experimentalists to the investigation of the existence of superheavy nuclei (SHN) beyond the valley of stability. The half lives of different radioactive decay such as alpha decay and spontaneous fission are the experimental signatures of the formation of SHN in fusion reaction. Hence, the calculations of these half-lives are important in identifying the decay chains of SHN. The existence of SHN is controlled mainly by spontaneous fission and  $\alpha$  decay processes. Hence identifying and characterizing the  $\alpha$  decay chains form a crucial part of nuclide identification in the synthesis of SHN.

In this paper we have presented a systematic study on the feasibility of observing alpha decay chains from the isotopes of the superheavy nuclei with  $Z = 115, 117, 118, 119$  and  $120$  has been performed using the recently proposed Coulomb and proximity potential model for deformed nuclei (CPPMDN) [1], the modified version of CPPM (Coulomb and proximity potential model) [2] incorporating quadrupole ( $\beta_2$ ) and hexadecapole ( $\beta_4$ ) deformation values of the both parent and daughter nuclei.

## The Model

The potential energy barrier in CPPMDN is taken as the sum of deformed Coulomb potential, deformed two-term proximity potential and the centrifugal potential, for the touching configuration and for the separated fragments. For the pre-scission region, a simple power law interpolation was used.

The Coulomb interaction between the two deformed and oriented nuclei is given as,

$$V_C = \frac{Z_1 Z_2 e^2}{r} + 3Z_1 Z_2 e^2 \sum_{\lambda, \mu=1,2} \frac{1}{2\lambda+1} \frac{R_{0i}^\lambda}{r^{\lambda+1}} Y_\lambda^{(0)}(\alpha_i) \left[ \beta_{2i} + \frac{4}{7} \beta_{2i}^2 Y_2^{(0)}(\alpha_i) \delta_{\lambda,2} \right] \quad (1)$$

with

$$R_i(\alpha_i) = R_{0i} \left[ 1 + \sum_{\lambda} \beta_{\lambda i} Y_\lambda^0(\alpha_i) \right] \quad (2)$$

Here  $R_{0i} = 1.28 A_i^{1/3} - 0.76 + 0.8 A_i^{-1/3}$  where  $\alpha_i$  is the angle between the radius vector and symmetry axis of the  $i^{th}$  nuclei. The two-term proximity potential for interaction between a deformed and spherical nucleus is given by Baltz et. al., as

$$V_{p2}(R, \theta) = 2\pi \left[ \frac{R_1(\alpha) R_C}{R_1(\alpha) + R_C + S} \right]^{1/2} \left[ \frac{R_2(\alpha) R_C}{R_2(\alpha) + R_C + S} \right]^{1/2} \times$$

$$\left[ \varepsilon_0(S) + \frac{R_1(\alpha) + R_C}{2R_1(\alpha)R_C} \varepsilon_1(S) \right] \left[ \varepsilon_0(S) + \frac{R_2(\alpha) + R_C}{2R_2(\alpha)R_C} \varepsilon_1(S) \right]^{1/2} \quad (3)$$

Here  $R_1(\alpha)$  and  $R_2(\alpha)$  are the principal radii of curvature of the daughter nuclei at the point where polar angle is  $\alpha$ ,  $S$  is the distance between the surfaces along the straight line connecting the fragments,  $R_C$  is the radius of the spherical cluster,  $\varepsilon_0(S)$  and  $\varepsilon_1(S)$  are the one dimensional slab-on-slab function. Using one dimensional WKB approximation, the barrier penetrability  $P$  is given as

$$P = \exp \left\{ -\frac{2}{\hbar} \int_a^b \sqrt{2\mu(V-Q)} dz \right\} \quad (4)$$

The turning points “ $a$ ” and “ $b$ ” are determined from the equation,  $V(a)=V(b)=Q$ . The half life time is given by

$$T_{1/2} = \left( \frac{\ln 2}{\lambda} \right) = \left( \frac{\ln 2}{\nu P} \right) \quad (5)$$

where,  $\nu = (\omega/2\pi) = (2E_v/\hbar)$ , represents the number of assaults on the barrier per second and  $\lambda$  the decay constant.  $E_v$  is the empirical vibration energy.

## Results and Discussion

Within CPPMDN, an extensive study on the feasibility of alpha decay from the isotopes of  $^{271-294}115, ^{270-301}117, ^{271-310}118, ^{274-313}119$  and  $^{272-319}120$  have been done. The energy released in the alpha transitions between the ground state energy levels of the parent nuclei and the ground state energy levels of the daughter nuclei is given as

$$Q_{gs \rightarrow gs} = \Delta M_p - (\Delta M_d + \Delta M_\alpha) + k(Z_p^\epsilon - Z_d^\epsilon) \quad (6)$$

where  $\Delta M_p, \Delta M_d, \Delta M_\alpha$  are the mass excess of the parent, daughter and alpha particle respectively. The  $Q$  values are evaluated using the mass excess values taken from Wang et al., and Koura-Tachibana-Uno-Yamada (KTUY). The term  $kZ^\epsilon$  represents the screening effect of atomic electrons.

Now, to identify the mode of decay of the isotopes under study, the spontaneous fission (SF) half lives have also been evaluated using the semi empirical relation of Xu *et al.*, given as

$$T_{1/2} = \exp \left\{ 2\pi \left[ C_0 + C_1 A + C_2 Z^2 + C_3 Z^4 + C_4 (N-Z)^2 - (0.13323 \frac{Z^2}{A^{0.5}} - 11.64) \right] \right\}$$

As this equation was originally made to fit the even-even nuclei, and as we have considered the odd mass (odd-even and odd-odd) nuclei, instead of taking spontaneous fission half life directly, we have taken the average of fission half life of the corresponding neighboring even-even nuclei as the case may be and our calculations show the agreement between experimental and computed average spontaneous fission half lives. Thus, those

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isotropes with small alpha decay half lives than the spontaneous fission half lives survive fission and hence can be detected through alpha decay in the laboratory. Thus by comparing the alpha decay half lives with the spontaneous fission half lives, we could identify the nuclei (both parent and decay products) that will survive fission.

The alpha decay half lives of  $^{271-294}_{115}$  superheavy nuclei, including the recently synthesized  $^{287}_{115}$  and  $^{288}_{115}$  have been calculated [3] within CPPMDN. On comparing the alpha decay half lives with the spontaneous fission half lives, we could predict 4 $\alpha$  chains from  $^{287}_{115}$  and 3 $\alpha$  chains from  $^{288}_{115}$ . As one may notice, our prediction agrees well with the experimental observations and it is also to be noted that the alpha half lives calculated using our formalisms matches well with the experimental alpha half lives. As we could successfully reproduce the experimental results in the case of  $^{287}_{115}$  and  $^{288}_{115}$ , we have confidently extended our work in predicting the  $\alpha$  decay half lives of 22 more superheavy elements of  $Z = 115$  with a view to find possible alpha decay chains and our study predicts 2 $\alpha$  chains from  $^{273,274,289}_{115}$ , 3 $\alpha$  chains from  $^{275,292}_{115}$ , 4 $\alpha$  chains consistently from  $^{284,285,286}_{115}$  nuclei and 5 $\alpha$  chains consistently from  $^{288-291}_{117}$ . We hope that these findings will provide a new guide for future experiments.

The alpha decay half lives of SHN with  $Z = 117$  have been evaluated [4,5] in a similar manner as mentioned above within CPPMDN. We have predicted 3 $\alpha$  chains for  $^{293}_{117}$  and 6 $\alpha$  chains for  $^{294}_{117}$  and it can be seen that our predictions go hand in hand with the experimental observations. Now, we have confidently extended our work in predicting the  $\alpha$  decay half lives of 32 more superheavy elements of  $Z = 117$  and our study reveals that those isotopes of  $Z = 117$  with  $A \geq 299$  and with  $A \leq 271$ , do not survive fission and thus the alpha decay is restricted within the range  $272 \leq A \leq 298$ . Through our study, we have predicted 1 $\alpha$  chain from  $^{272,273,296-298}_{117}$ , 2 $\alpha$  chains from  $^{274,275,295}_{117}$ , 3 $\alpha$  chains from  $^{276,277,292}_{117}$  and 5 $\alpha$  chains from  $^{288-291}_{117}$ .

The alpha decay half lives of SHN with  $Z = 118$  and  $Z = 119$  have also been evaluated [6,7] in a similar manner within CPPMDN. The  $\alpha$  decay half-lives and the mode of decay of  $^{294}_{118}$  evaluated using our formalisms, were found to be in good agreement with the experimental results. Now, we have confidently extended our work in predicting the  $\alpha$  decay half lives of 39 more superheavy elements of  $Z = 118$  and our study reveals that those isotopes of  $Z = 118$  with  $A \geq 301$  and with  $A \leq 275$ , do not survive fission and thus the alpha decay is restricted within the range  $276 \leq A \leq 300$ . Through our study, we have predicted 1 $\alpha$  chain from  $^{276,298-300}_{118}$ , 2 $\alpha$  chains from  $^{277,278,295-297}_{118}$  and 5 $\alpha$  chains from  $^{289-293}_{118}$ . Even though we could

Phys. 60s(2005) consistent 3 $\alpha$ , 4 $\alpha$ , and 6 $\alpha$  chains from  $^{279,280}_{118}$ ,  $^{281}_{118}$ , and  $^{282,283}_{118}$ , respectively, these nuclei could not be predicted to be synthesized in the laboratories as their decay half-lives are too small, which span the order  $10^{-9}$ s to  $10^{-6}$ s. The study on  $^{274-313}_{119}$  helps to identify the mode of decay of about 40 isotopes with  $Z = 119$ . Our reveals that those isotopes of  $Z = 119$  with  $A \geq 309$  and with  $A \leq 275$  do not survive fission, and thus, the  $\alpha$  decay is restricted within the range of  $276 \leq A \leq 308$ . Through our study, we have predicted 6 consistent  $\alpha$  chains from  $^{292-295}_{119}$ , 5 consistent  $\alpha$  chains from  $^{296}_{119}$ , 4 consistent  $\alpha$  chains from  $^{297}_{119}$ , and 3 consistent  $\alpha$  chains from  $^{298,299}_{119}$  which will be a new guide for future experiments.

The predictions on the  $\alpha$  decay chains of  $^{272-319}_{120}$  SHN have also been done [8] within CPPMDN. The study reveals that the  $\alpha$  decay half lives and the mode of decay of the isotopes of the experimentally synthesized SHN  $^{298,299}_{120}$  evaluated using our formalism agree well with the experimental observations. Our study on predicts that the  $\alpha$  decay is restricted within the range  $277 \leq A \leq 308$  as those isotopes with  $A \leq 276$  and those nuclei with  $A \geq 309$  do not survive fission. We have also forecasted the mode of decay of  $^{288-302}_{120}$  superheavy nuclei as 6 $\alpha$  chains from the nuclei of  $^{288,289,291-295}_{120}$ , 7 $\alpha$  chains from  $^{290}_{120}$ , 5 $\alpha$  chains from  $^{296,297}_{120}$ , and 3 $\alpha$  chains from  $^{300-302}_{120}$ , which could be of great interest to the experimentalists.

The alpha half life calculations have also been done using the CPPM formalism, the Viola-Seborg semi-empirical relationship (VSS), the Universal curve (UNIV) of Poenaru et al., and the analytical formulae of Royer and it could be seen that the alpha decay half lives evaluated using our formalism agrees well with the values evaluated using these theoretical formalisms.

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