

Determination of breakup probability P_{BU} in ${}^9\text{Li}+{}^{208}\text{Pb}$ reaction within the dynamical cluster-decay model.

Arshdeep Kaur* and Raj K. Gupta

Department of Physics, Panjab University, Chandigarh - 160014, INDIA

Introduction

The compound nucleus (CN) ${}^{217}\text{At}^*$, formed by projecting neutron-rich ${}^9\text{Li}$ on doubly magic ${}^{208}\text{Pb}$, is studied within the dynamical cluster-decay model (DCM) [1] at various center-of-mass energies. Here, in this work, we concentrate on this system at $E_{c.m.}=28.5$ MeV, corresponding to temperature $T=1.145$ MeV, where experimental [2] isotopic yields of only heavy mass residues ${}^{213,214}\text{At}$, i.e., the light-particles (LPs) evaporation residue (ER) cross sections σ_{xn} for $x=3,4$ neutrons emission, are measured with fusion-fission (ff) component σ_{ff} taken to be zero.

${}^9\text{Li}$ is a neutron-rich, weakly bound nucleus, and the fusion cross sections for such projectiles are expected to get enhanced due to the extended neutron density profile or the large neutron-skin. Our DCM calculations [1] show that the CN cross section σ_{CN} is negligibly small, compared to the competing non-compound nucleus (nCN) content σ_{nCN} , comprising the processes like that of quasi fission (qf), incomplete fusion (ICF), or deep inelastic collisions (DIC), etc.. Thus, the total fusion cross section $\sigma_{fusion} = \sigma_{CN} + \sigma_{nCN}$. Alternatively, in the following we look for the projectile breakup effects, in competition to its fusion.

Methodology

A. Dynamical cluster-decay model

The Dynamical cluster-decay model (DCM) of Gupta and Collaborators [3, 4] is the non-statistical description of the dynamical mass motion of preformed clusters through the interaction barriers which treat all types of CN

decays, i.e., ER's or LPs ($A_2 \leq 4$), IMFs ($5 \leq A_2 \leq 20$) and ff fragments on the same level (IMFs are a part of ff), in contrast to statistical models where each type of decay (ER or ff) is treated on different footings. The decay of a hot and rotating CN in the DCM is worked out in terms of the decoupled relative separation R and mass (and charge) asymmetries $\eta=(A_1-A_2)/(A_1+A_2)$ (and $\eta_Z=(Z_1-Z_2)/(Z_1+Z_2)$) coordinates, defining the CN decay cross section for ℓ partial waves as

$$\sigma_{A_1,A_2} = \frac{\pi}{k^2} \sum_{\ell=0}^{\ell_{max}} (2\ell+1)P_0P; \quad k = \sqrt{\frac{2\mu E_{c.m.}}{\hbar^2}} \quad (1)$$

Here, P_0 is the preformation probability, referring to η -motion and P , the penetrability, to R -motion. μ is the reduced mass with m as the nucleon mass. ℓ_{max} is the maximum angular momentum, defined for $\sigma_{ER} \rightarrow 0$. Eq. (1) gives $\sigma_{ER} = \sum_{A_2=1}^4 \sigma_{(A_1,A_2)} = \sum_{x=1}^4 \sigma_{xn}$, $\sigma_{ff} = 2 \sum_{A_2=5}^{A/2} \sigma_{(A_1,A_2)}$, and their sum $\sigma_{CN} (= \sigma_{ER} + \sigma_{ff})$. Also, Eq. (1) gives σ_{nCN} , calculated as the quasi-fission (qf)-like decay where $P_0=1$, i.e, for σ_{nCN} we use DCM($P_0=1$) and in case the σ_{nCN} were not measured, it can be estimated empirically, as $\sigma_{nCN} = \sigma_{fusion}^{Expt.} - \sigma_{CN}^{Cal.}$.

Having defined the relevant σ 's in the DCM, we can write the statistical CN fusion/ formation probability P_{CN} [3], and the CN survival probability P_{surv} [4] against fission, i.e., the probability of fused system to de-excite by emission of neutrons or LPs, equivalently, the ER, rather than fission, each given by

$$P_{CN} = \frac{\sigma_{CN}}{\sigma_{fusion}} = 1 - \frac{\sigma_{nCN}}{\sigma_{fusion}}, \quad (2)$$

$$P_{surv} = \frac{\sigma_{ER}}{\sigma_{CN}} = 1 - \frac{\sigma_{ff}}{\sigma_{CN}}, \quad (3)$$

*Electronic address: arshdeep.pu@gmail.com

P_{CN} takes care of the nCN effects, and P_{surv} of the ff process. In other words, $P_{CN}=1$ if $\sigma_{nCN}=0$, and $P_{surv}=1$ if $\sigma_{ff}=0$.

B. Estimation of breakup probability

The statistical relations above allow us to write for CN process, the ER cross section as [5, 6]:

$$\sigma_{ER}^{CN} = \sum_{\ell=0}^{\ell_{max}} \sigma_{fusion} P_{CN} P_{surv}. \quad (4)$$

For fusion studies involving weakly bound nuclei, if breakup (BU) occurs in competition with fusion, we can define the breakup Probability P_{BU} as:

$$P_{BU} = 1 - P_{CN} \quad (5)$$

Thus, P_{BU} is the probability that the projectile BU rather than fuse. Then, from Eq. (4), the ER cross-section for breakup is

$$\sigma_{ER}^{BU} = \sum_{\ell=0}^{\ell_{max}} \sigma_{fusion} P_{BU} P_{surv}. \quad (6)$$

so that the total ER cross section (σ_{ER}^{total}) is the sum of σ_{ER}^{CN} and σ_{ER}^{BU} . Note, however, that if σ_{nCN} were a measured quantity, like the qf process, then for BU to occur,

$$P_{BU} = 1 - (P_{CN} + P_{nCN}) \quad (7)$$

In the present reaction under study, however, σ_{nCN} is determined empirically, and hence Eq. (5) is valid.

Calculations and Results

Table I gives the ER cross sections for the CN and BU processes, calculated by using Eqs. 4 and 6, respectively, with their sum giving σ_{ER}^{total} ($=\sigma_{ER}^{CN} + \sigma_{ER}^{BU}$) which is comparable with the experimental data. In Fig.1, we have shown the variation of P_{CN} , P_{BU} and σ_{fusion} ($=\sigma_{CN} + \sigma_{nCN}$) as a function of angular momentum for 3n and 4n decay channels. Fig. 1 shows the expected behavior of P_{CN} and P_{BU} as complimentary processes. Evidently, the

main contribution to σ_{ER}^{total} is from σ_{ER}^{BU} , i.e., σ_{ER}^{BU} ($\equiv\sigma_{nCN}$) contribution to the total fusion cross section is large.

TABLE I: The DCM calculated ER cross sections for CN and BU processes, compared with the experimental value. Note, $P_{surv}=1$ since $\sigma_{ff}=0$.

Decay Channel	σ_{ER}^{CN} (mb)	σ_{ER}^{BU} (mb)	σ_{ER}^{total} (mb)	$\sigma_{ER}^{Expt.}$ (mb)
$^{217}\text{At}^* \rightarrow ^{214}\text{At}+3\text{n}$	0.09	8.31	8.4	8.4 ± 1.9
$^{217}\text{At}^* \rightarrow ^{213}\text{At}+4\text{n}$	0.74	68.6	69.34	$69.3 \pm 8.$

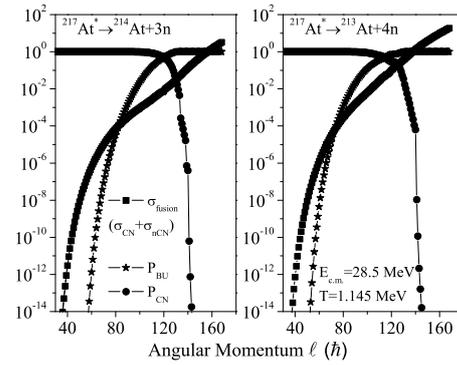


FIG. 1: The DCM calculated P_{CN} , P_{BU} and σ_{fusion} ($=\sigma_{CN} + \sigma_{nCN}$) for 3n and 4n decay channels as a function of angular momentum.

References

- [1] A. Kaur, B. R. Behera, and R. K. Gupta, Proc. the DAE-BRNS Symp. on Nucl. Phys. **60**, 480 (2015).
- [2] A. M. Vinodkumar *et al.*, Phys. Rev. C **80**, 054609 (2009).
- [3] A. Kaur, S. Chopra, and R. K. Gupta, Phys. Rev. C **90**, 024619 (2014).
- [4] S. Chopra, A. Kaur, and R. K. Gupta, Phys. Rev. C **91**, 034613 (2015).
- [5] A. M. Vinodkumar *et al.* Phys. Rev. C **87**, 044603 (2013).
- [6] S. Chopra, A. Kaur, Hemdeep and R. K. Gupta, Phys. Rev. C **93**, 044604 (2016).