

## Influence of the functional form of the Finite range interaction in the predictions of finite Nuclei

P. Bano<sup>1</sup>, C. Gonzalez-Boquera<sup>2</sup>, T. R. Routray<sup>1\*</sup>, X. Viñas<sup>2</sup>, M. Centelles<sup>2</sup> and D. Behera<sup>1</sup>

<sup>1</sup> School of Physics, Sambalpur University, Jyotivihar-768 019, India

<sup>2</sup>Departament de Física Quàntica i Astrofísica and Institut de Ciències del Cosmos (ICCUB), Facultat de Física, Universitat de Barcelona, Martí i Franquès 1, E-08028 Barcelona, Spain

\* email: \*trr1@rediffmail.com

### Introduction

The finite range Simple effective interaction (SEI) has been used in the studies of various aspects of nuclear matter (NM) [1-3]. Nine parameters from the combinations of altogether eleven parameters of SEI required for complete study of asymmetric nuclear matter (ANM) have been adjusted carefully using minimum number of experimental/empirical constraints. The predictions of SEI in the areas of the momentum and density dependence of the mean field in NM are in conformity with the trend predicted by microscopic calculations. The use of SEI has been extended to the finite nuclei study with the Gaussian form for its finite range part. The two open parameters of SEI, taken to be  $t_0$  and  $x_0$  along with the additional spin-orbit (SO) interaction strength parameters  $W_0$  (in case of finite nucleus) are to be fixed for the study of finite nuclei. Out of the three open parameters,  $t_0$ ,  $x_0$  and  $W_0$ , the parameter  $x_0$  has been fixed from the spin-polarization property of pure neutron matter (PNM), and the rest two parameters  $t_0$  and  $W_0$  are fixed from the fits to the binding energies (BEs) of doubly closed nuclei  $Ca^{40}$  and  $Pb^{208}$  [4]. All the eleven plus the  $W_0$  – parameters fixed from the NM and finite nuclei, could reproduce the BEs of 161 and charge radii of 86-spherical even-even nuclei within root mean square deviations (rms)  $\sim 1.5$  MeV and  $\sim 0.015$  fm, respectively, with the Gaussian form of SEI [4,5]. The SEI with its Gaussian form has also been used in the study of fission dynamics [6]. In this work we present some results of finite nuclei study with SEI having Yukawa form for its finite range part. The study will show the influence of the functional form of the interaction in the predictions of finite nuclei properties.

### Formalism

The finite range Simple effective interaction is given by,

$$V(\vec{r}) = t_0(1 + x_0 P_\sigma)\delta(\vec{r}) + \frac{t_3}{16}(1 + x_3 P_\sigma)\left(\frac{\rho(\vec{r})}{1 + b\rho(\vec{r})}\right)^\tau \delta(\vec{r}) + (W + B P_\sigma - H P_\tau - M P_\sigma P_\tau)f(r) \quad (1)$$

where,  $f(r) = \frac{e^{-r/\alpha}}{r/\alpha}$  is the finite range part taken

to be of Yukawa form. The procedure of determination of eleven parameters  $b, \alpha, \gamma, t_0, x_0, t_3, x_3, W, B, H$  and  $M$  plus the SO strength parameter  $W_0$  is similar to that of the Gaussian form of SEI discussed in [4, 5]. The finite nuclei study has been carried out in the framework of Density Functional Theory (DFT) where the non-local density matrix  $\rho\left(\vec{r}, \vec{r}'\right)$  has been

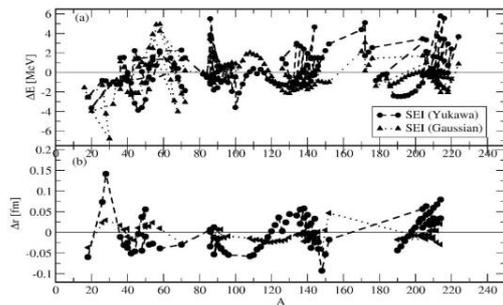
localized by using the Semi-Classical  $\hbar^2$ -expansion. The SO interaction has been taken similar to the Skyrme case. The pairing interaction has been taken in the BCS framework by using a contact interaction whose parameter has been adjusted to the energy gap in PNM. The general expression of the localized density matrix  $\rho\left(\vec{r}, \vec{r}'\right)$  under  $\hbar^2$ -expansion, that is

applicable to both Gaussian and Yukawa form of finite range interactions, is given in equation (A1) of [7].

### Result and Discussions

The Equation of State (EOS) of SEI used for calculations of finite nuclei results is for  $\gamma=1/2$  that predicts NM incompressibility  $K(\rho_0) \sim 240$  MeV. The open parameters  $t_0$  and  $W_0$  are determined from fits to the BEs of  $Ca^{40}$  and  $Pb^{208}$ . The BEs of 161- and charge radii of 86-

even-even spherical nuclei have been calculated. It is worth mentioning that for a given stiffness of NM, i.e., given  $\gamma$ , in order to get the best prediction in terms of minimum rms deviation, the NM saturation properties, namely, the saturation density  $\rho_0$  and the symmetry energy at saturation density  $E_s(\rho_0)$  are to be varied within their accepted range. For the EOS  $\gamma=1/2$  the NM saturation properties for which minimum rms deviations in the results of BE and charge radii are obtained, is given in Table 1. It has been noticed that in the predictions BE and charge radii, the values of  $E_s(\rho_0)$  and  $\rho_0$  play a dominant role, whereas the influence of energy per particle is minimum. The results of the BEs of 161- and charge radii of 86- spherical even-even nuclei for the EOS  $\gamma=1/2$  of SEI having Yukawa form have been given in the panels (a) and (b) of Fig. 1. The rms deviations for the BE is  $\Delta E = 1.9$  MeV, whereas, that of charge radii,  $\Delta r = 0.04$  fm.



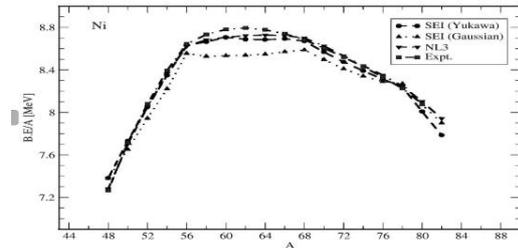
**Fig.1** rms deviation of BE of 161 even-even spherical nuclei in panel (a) and rms deviation of charge radii of 86-spherical even-even nuclei in panel (b) for Yukawa and Gaussian form of SEI.

Form of SEI	$e(\rho_0)$ (MeV)	$\rho_0$ ( $\text{fm}^{-3}$ )	$E_s(\rho_0)$ (MeV)	$L(\rho_0)$ (MeV)
Yukawa	-16.05	0.163	34	72.66
Gaussian	-16	0.158	35.5	76.71

**Table 1.** Nuclear matter Saturation properties of the two sets of EOS of SEI having Yukawa and Gaussian form.

In order to examine the influence of the functional form of the finite range part, we have made the calculation for the equivalent EOS of SEI having Gaussian form. The equivalent EOS of SEI with Gaussian form has been obtained by matching the NM incompressibility values, and this has been obtained for the value of  $\gamma=0.42$ . The results of BEs and charge radii for the Gaussian form are also given in the respective

panels of Fig. 1. The comparison between the predictions of BEs and charge radii under DFT formulation for Yukawa and Gaussian forms of SEI shows that the later one is more competent for the bulk properties of nuclei. In order to explore the consequence of the finding we have computed the results of BEs in the isotopic chain of Ni-isotopes using both forms of SEI. The results of BE/A along with the NL3 and experimental values are given in the Fig. 2.



**Fig.2** BEs in the isotopic chain of Ni-isotopes using both forms of SEI compared with NL3 and experimental data.

### Conclusion

It is found that under DFT formulation where the density matrix is localized by using the semi-classical  $\hbar$  - expansion up to second order i.e., up to  $\hbar^2$  - term, the Gaussian form of SEI reproduces the BEs and charge radii of spherical nuclei quite well. However, under the same formulation the Yukawa form of SEI fails to reproduce charge radii well as compared to its Gaussian counterpart, whereas, the BEs are reproduced with rms deviation in close proximity with that of the Gaussian form.

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