

## Pion multiplicity fluctuations in p-p collisions at $\sqrt{S_{nn}} = 13$ TeV

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### Introduction

In relativistic heavy ion collisions, the existence of large fluctuations in pseudo-rapidity space have been followed in cosmic ray JACEE[1] events and in different types of accelerator and collider experiments. It is evident that the intermittent fluctuations are nothing but the results of QGP phase transition. There are different types of method to identify such types of fluctuation for long range or short range  $\eta$  distribution. In order to study multiplicity fluctuations depending on the scale factorial moments, Bialas and Peschanski[1] gave an excellent idea about the scale factorial moments. He showed the dependency of scaled factorial moments on power law dividing the phase space into a pseudo-rapidity bin width. This scale factorial moments are known as intermittency.

### 1. Methodology

In one dimensional  $\eta$  space, the factorial moments  $F_q$  of order  $q$  is defined as

$$F_q = M^{q-1} \sum_{m=1}^M \frac{\langle n_m(n_m - 1) \dots (n_m - q + 1) \rangle}{n_m^q} \quad (1)$$

Where  $M$  is the number of bins in  $\eta$  space and  $n_m$  is the number of particles in  $m^{th}$  bin. In presence of intermittency the factorial moment shows power like growths, i.e

$\langle F_q \rangle \propto M^{\alpha_q}$  and  $\ln \langle F_q \rangle = \alpha_q \ln M + c$   
Where  $c$  is constant and we can get the value of  $\alpha_q$  from this linear fit graph.  $\alpha_q > 0$  and it is known as intermittency exponent. Now  $\lambda_q$

is the strength of the intermittency, can also be obtained from  $\alpha_q$

$$\lambda_q = \frac{\alpha_q + 1}{q} \quad (2)$$

Depending on the value of  $\lambda_q$  we will come to know whether the non-thermal phase transition is possible or not. The fractal dimension  $d_q$  [2, 3] can also be obtained as

$$d_q = \frac{\alpha_q}{q - 1} \quad (3)$$

Now we have calculated the value of  $\beta_q$  which is the ratio of higher order fractal dimension( $d_q$ ) to the second order fractal dimension( $d_2$ )[4]

$$\beta_q = \frac{d_q}{d_2} (q - 1) \quad (4)$$

We have also calculated the value of critical exponent  $\gamma$

$$\beta_q = (q - 1)^\gamma \quad (5)$$

From the value of  $\gamma$  we can get the idea about the quark-hadron phase transition.

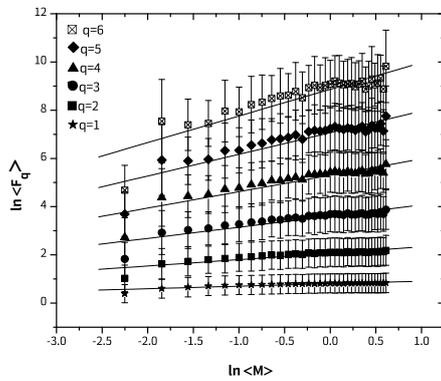
### 2. Result and discussion

In order to know the existence of non thermal and quark hadron phase transition we have analysed the variation of  $\langle F_q \rangle$  with respect to  $M$  for order of  $q$  ( $q=1,2,3,4,5,6$ ) for the multiplicity of pp collisions at  $\sqrt{S_{nn}} = 13$  TeV. To generate the data sample we have used the Ultra Relativistic Quantum Molecular Dynamics (UrQMD). In fig.1 we have plotted  $\ln \langle F_q \rangle$  vs  $\ln M$  graph and we have seen that factorial moment  $F_q$  is increasing with increasing the number of bins for each value of  $q$  in one dimensional  $\eta$  space.

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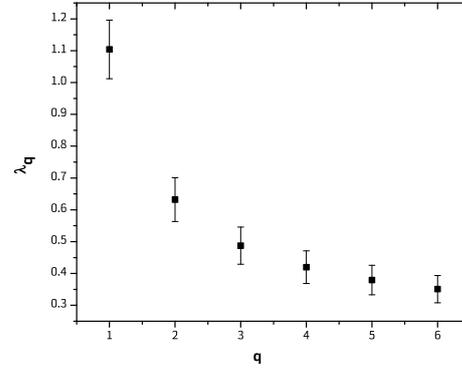
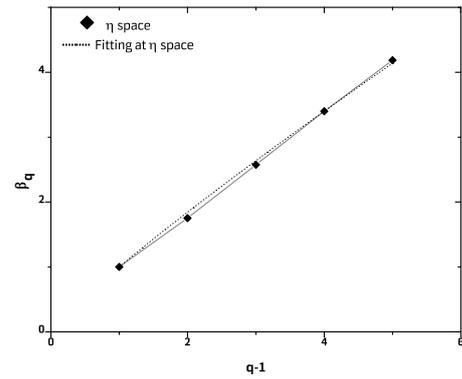
TABLE I: Data of different parameters depending on the factorial moment analysis.

q	$\alpha$	$\lambda$	$d_q$	$\beta_q$
1.0	0.1041 $\pm 0.09198$	1.1041 $\pm 0.09198$		
2.0	0.26393 $\pm 0.13737$	0.63197 $\pm 0.068685$	0.26393 $\pm 0.13737$	1.00 $\pm 0.27474$
3.0	0.46226 $\pm 0.17474$	0.4874 $\pm 0.05825$	0.23113 $\pm 0.08737$	1.7514 $\pm 0.22474$
4.0	0.67929 $\pm 0.20548$	0.4198 $\pm 0.05137$	0.22643 $\pm 0.06849$	2.5738 $\pm 0.20586$
5.0	0.89684 $\pm 0.23257$	0.0.3794 $\pm 0.04651$	0.22421 $\pm 0.05815$	3.3980 $\pm 0.19552$
6.0	1.10435 $\pm 0.25789$	0.3507 $\pm 0.04298$	0.22087 $\pm 0.05158$	4.1843 $\pm 0.18895$


 FIG. 1:  $\ln \langle F_q \rangle$  vs  $\ln M$  in  $\eta$  space.

Depending on this graph we have also calculated  $\alpha_q$ ,  $\lambda_q$ ,  $\beta_q$  and  $\gamma$  which are listed below.

From fig.2 we have observed the variation of  $\lambda_q$  with respect to  $q$ . It is seen that  $\lambda_q$  is decreasing with increasing  $q$  but does not show any distinct lower value which indicates that there is no non thermal phase transition in the multiplicities of the charged particles. From fig.3 we have seen the variation of  $\beta_q$  with respect to  $(q-1)$ . This variation follows a straight line path and it is fitted with the equation  $\beta_q = (q-1)^\gamma$ . Depending on the above table we have also found the value of critical exponent  $\gamma=0.88$ . According to the GL theory if the value of critical exponent  $\gamma$  is around 1.304, then there must exist the quark-hadron phase transition. Therefore depending on our data analysis we have seen that the value of  $\gamma$  is far away from 1.304. Now


 FIG. 2:  $\lambda_q$  with  $q$  in 1dimensional  $\eta$  space.

 FIG. 3: Variation of  $\beta_q$  with  $q-1$  in  $\eta$  space.

we can easily conclude that there is no quark-hadron phase transition in the multiplicities of the pp collisions.

## References

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