

## Dynamical description of nuclear dissipation through decay of $^{248}\text{Cf}$ using one-dimensional Langevin dynamical model

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### Introduction

Fission dynamics is necessary in many areas of physics such as nuclear astrophysics applications and studies related to the production of superheavy nuclei. A comprehensive understanding of this process is still missing due to the complex nature of the nuclear interactions. The time evolution of a fissioning nucleus can only be realized once the associated theoretical model is validated with the measured data. The measurement of the pre-scission particle multiplicities and giant dipole resonance (GDR)  $\gamma$ -ray multiplicities are important observables to investigate fission dynamics. Moreover, pre-scission neutron multiplicity is also used as a clock to measure fission lifetime [1].

The pre-scission neutron multiplicity was measured for the reaction  $^{16}\text{O}+^{232}\text{Th}$  populating the compound nucleus (CN)  $^{248}\text{Cf}$ , measured earlier by Saxena *et al.* [2], and systematic analysis of the pre-scission neutron multiplicity was carried out. It was observed that the formation delay depends on the entrance channel mass asymmetry relative to the Businaro–Gallone point. The statistical model study of the decay of  $^{248}\text{Cf}$  is already done by Banerjee *et al.* [3]. Since the dynamical effects play a crucial role in the fission process, we, therefore, want to study the nuclear dissipative properties through decay of  $^{248}\text{Cf}$  by using a one-dimensional Langevin dynamical model. The dynamical model calculation has been performed for the reaction  $^{16}\text{O}+^{232}\text{Th}$  at three excitation energies 49.5,

55.2, and 60.8 MeV, for which the experimental data of pre-scission neutron multiplicity ( $\nu_{pre}$ ) is already measured [2].

### Dynamical Model Calculations

The time evolution of the compound nuclei is studied by using a one-dimensional Langevin dynamical model governed by the Langevin equations,

$$\begin{aligned} \frac{dp}{dt} &= \frac{p^2}{2} \frac{d}{dc} \left( \frac{1}{\mathcal{M}} \right) - \frac{dF}{dc} - \frac{\eta}{\mathcal{M}} p + g\Gamma(t), \\ \frac{dc}{dt} &= \frac{p}{\mathcal{M}}, \end{aligned} \quad (1)$$

where  $c$  is the collective coordinate defining the deformation of a fissioning nucleus, and  $p$  is the collective momentum conjugate to  $c$ .

The shape-dependent collective inertia  $\mathcal{M}(c)$  is calculated by employing the Werner-Wheeler prescription.  $F(c)$  represents the Helmholtz free energy and it is calculated from the double-folding Yukawa-plus-exponential potential  $V(c)$  by relation  $F(c) = V(c) - (a(c) - a(0))T^2$ . Here,  $a(c)$  is the shape dependent level density parameter and  $a(0)$  being its value for the spherical shape ( $c = 1$ ) [4].  $T$  is the Fermi-gas temperature corresponding to the spherical shape represented as  $T = \sqrt{E^*/a(0)}$ . The strength of the random force  $g(c)$  is related to the dissipation coefficient  $\eta(c)$  through the fluctuation-dissipation theorem:  $g(c) = \sqrt{\eta(c)T}$ . The time-dependent part of the random force follows the time correlation property:  $\langle \Gamma(t)\Gamma(t') \rangle = 2\delta(t - t')$ . A Langevin trajectory is considered as a fission event when  $c$  reaches the scission configuration, i.e.,  $c = 2.01$ , and the corresponding time is called the fission-time  $\tau_f$ .

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## Results and Discussion

The experimental values of the  $\nu_{pre}$  are reproduced with different choices like the chaos-weighted wall friction and wall+window friction (WF) with different values of the reduction factor  $k_s$ , which is shown in Fig. 1. The chaos-weighted wall friction was not able to reproduce the experimental value of  $\nu_{pre}$  at any excitation energy. The wall + window friction with reduction factor  $k_s = 0.5$  has reproduced the experimental value of  $\nu_{pre}$  at excitation energy of 49.5 MeV, and reduction factor  $k_s = 0.75$  is required at 55.2 MeV excitation energy. We were not able to reproduce the experimental value of  $\nu_{pre}$  at 60.8 MeV excitation energy with wall + window friction description.

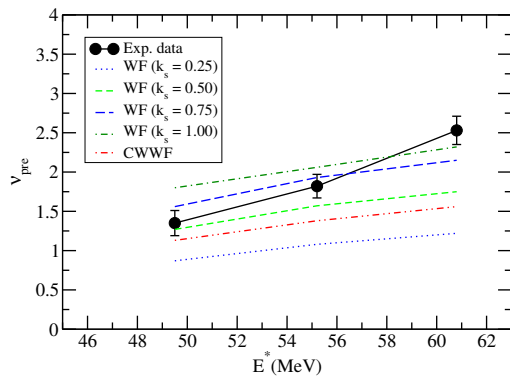


FIG. 1: Experimental values of  $\nu_{pre}$  are compared with corresponding dynamical results for different type of dissipation strength.

Further, we performed calculations with the shape independent reduced dissipation  $\beta$  ( $\beta = \eta/M$ ) as a free parameter, which is shown in Fig. 2. As shown in Fig. 2(a),  $\beta = 4$  MeV/ $\hbar$  provides good agreement with the experimental data at excitation energy 49.5 MeV, and for the excitation energies 55.2 and 60.8 MeV the values of the  $\beta$  are 5 and 8 MeV/ $\hbar$  respectively. Figure 2(b) shows the variation of the shape independent reduced dissipation  $\beta$  with respect to the excitation energy, required to reproduce the experimental value of  $\nu_{pre}$  at a particular excitation energy.

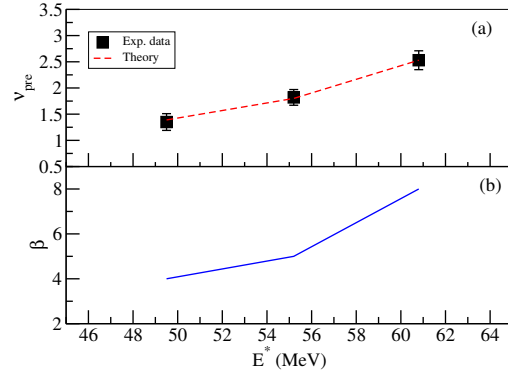


FIG. 2: (a) Experimental values of  $\nu_{pre}$  (squares), and calculated  $\nu_{pre}$  for  $^{16}\text{O}+^{232}\text{Th}$  (dashed lines). The  $\beta$  used for the dynamical model calculations is shown in (b) for each energy point.

In the present study, the dynamical decay of the  $^{248}\text{Cf}$  is studied considering chaos-weighted wall friction, wall+window friction (WF), and shape independent reduced dissipation. The wall+window friction (WF) with different values of the reduction factor  $k_s$  was able to reproduce the experimental data of  $\nu_{pre}$ , while chaos-weighted wall friction was not able to reproduce the experimental value of  $\nu_{pre}$ . It has also been observed that the shape independent reduced dissipation  $\beta$  is energy dependent for the present study.

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