

# Alpha and Cluster Decay studies of $^{207,208}\text{Th}$ Isotopes

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## Introduction

Heavy nuclei are found to be unstable and decay through various modes like spontaneous fission, alpha decay and cluster radioactivity. The  $\alpha$ -decay studies have important role in the development of nuclear physics. It can be described by the quantum tunneling effect through a potential barrier. The spontaneous emission of a nucleus heavier than alpha particle, but lighter than mass of a fragment in fission is known as Cluster radioactivity.

The Cluster Radioactivity was first predicted in 1980 by Sandulescu, Poenaru and Greiner [1] and then it was experimentally confirmed by Rose and Jones in 1984 for the  $^{14}\text{C}$  radioactivity from  $^{223}\text{Ra}$  [2]. Theoretical models including alpha particle emission model and nuclear fission model are used to explain cluster radioactivity.

The Coulomb and proximity potential model (CPPM) proposed by Santhosh et al. [3,4] has been used extensively for the studies in the areas of alpha decay, cluster decay and spontaneous fission of heavy and superheavy nuclei.  $^{207}\text{Th}$  was experimentally produced recently by directing  $^{36}\text{Ar}$  to  $^{176}\text{Hf}$ .  $^{207,208}\text{Th}$  are highly unstable and decay via spontaneous fission or alpha decay [5]. The synthesized heavy isotopes are identified by observing their alpha decay chains.

## The theoretical framework

In CPPM, the interaction potential barrier for a parent nucleus undergoing cluster decay is given as;

$$V = \frac{Z_1 Z_2 e^2}{r} + V_p(z) + \frac{\hbar^2 l(l+1)}{2\mu r^2} \text{ for } z > 0$$

where  $Z_1$  and  $Z_2$  are the atomic numbers of daughter and emitted cluster; ' $r$ ' is the distance

between fragment centers,  $l$  the angular momentum,  $\mu$  the reduced mass and  $V_p$  is the proximity potential.

The proximity potential is given as;

$$V_p(z) = 4\pi\gamma b \left[ \frac{C_1 C_2}{(C_1 + C_2)} \right] \Phi\left(\frac{z}{b}\right)$$

The turning points 'a' and 'b' are given by  $V(a) = V(b) = Q$ , where  $Q$  is the energy released. The half-life time is given by;

$$T_{1/2} = \frac{\ln 2}{\lambda} = \frac{\ln 2}{\nu P}$$

where,  $\nu = 2E_\nu/\hbar$ , represent the number of assaults on the barrier per second and  $E_\nu$ , the empirical zero-point vibration energy.

The Universal Decal Law (UDL)[6] can predict the lighter and heavier cluster emissions because of the inclusion of the preformation and fission like mechanisms. The UDL formula is given as;

$$\log_{10} T_{1/2} = aZ_c Z_d \sqrt{\mu} Q_c^{-1/2} + b \sqrt{\mu Z_c Z_d (A_c^{1/3} + A_d^{1/3})} + c$$

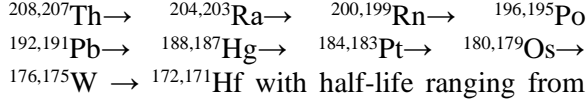
Here  $a = 0.4314$ ,  $b = -0.4087$  and  $c = -25.7725$ .  $Z_c$  and  $Z_d$  are mass numbers and  $A_c$  and  $A_d$  are atomic numbers of cluster and daughter.

## Results and Discussions

In this study we have computed the half-lives of alpha decay chain of  $^{207}\text{Th}$  and  $^{208}\text{Th}$  using CPPM. Obtained values are compared with half-lives values calculated based on UDL. The alpha decay energy  $Q_\alpha$  released during decay is calculated using the mass excess of the parent, daughter and  $\alpha$ -particle taken from the KTUY table.

$Q = \Delta M_p - (\Delta M_\alpha + \Delta M_d) + k(Z_p^e - Z_d^e)$ . Here  $\Delta M_p$ ,  $\Delta M_d$ , and  $\Delta M_\alpha$  represent the mass excess of the parent, daughter, and the  $\alpha$  particle respectively.  $k(Z_p^e - Z_d^e)$  is the term related with

electron screening effect on the energy of  $\alpha$  particle. Being very small this factor is neglected in our calculation. As per our calculation it was observed that the decay of  $^{208,207}\text{Th}$  follows the decay chain



with half-life ranging from around  $10^{-1}$  seconds to  $10^{20}$ seconds. Half-life values of the  $\alpha$ -decay chain up to Pb are shown in Table 1 and Table 2. From calculations it was observed that the half-life obtained by using CPPM and UDL formula agree with each other. The experimental values are also given in table for comparison.

**Table 1:**  $\alpha$  decay chain of  $^{207}\text{Th}$  isotope

	Q (MeV)	$\log_{10} T_{1/2}$ (sec)		
		CPPM	UDL	Expt.
$^{207}\text{Th}$	7.79	-0.75317	-1.2335	-2.01
$^{203}\text{Ra}$	7.74	-1.40503	-1.8819	-1.44
$^{199}\text{Rn}$	7.13	-0.0348	-0.5397	-0.23
$^{195}\text{Po}$	6.76	0.53058	0.00951	0.67
$^{191}\text{Pb}$	5.45	5.68647	5.08575	.....

**Table 2:**  $\alpha$  decay chain of  $^{208}\text{Th}$  isotope

	Q (MeV)	$\log_{10} T_{1/2}$ (sec)		
		CPPM	UDL	Expt.
$^{208}\text{Th}$	7.96	-1.3628	-1.8297	-2.36
$^{204}\text{Ra}$	7.64	-1.1044	-1.5552	-1.22
$^{200}\text{Rn}$	6.86	-1.0772	0.4899	0.04
$^{196}\text{Po}$	6.85	0.068	-0.3633	0.75
$^{192}\text{Pb}$	5.22	6.8471	6.3434	.....

The cluster decay half-life of  $^{207}\text{Th}$  and  $^{208}\text{Th}$  isotopes are estimated using the CPPM by inputting the Q-value determined using the KTUY mass table. Of the 104 examined possible clusters, the cluster decay half-lives corresponding to the emission of  $^8\text{Be}$ ,  $^{12,13}\text{C}$ ,  $^{16}\text{O}$  are found to be much less than the experimental upper limit of  $10^{30}$  seconds. Hence there is the probability for emission of these clusters from

$^{207}\text{Th}$  and  $^{208}\text{Th}$ . The half-life for alpha and cluster emission are also determined using UDL and compared with the predictions of the CPPM. A few results of our calculations are presented Tables 3 and 4. From the tables, one can notice that the predictions of the CPPM and the UDL formula are in good agreement.

**Table 3:** Cluster decay half-lives of  $^{207}\text{Th}$  isotope.

Cluster	Daughter	Q (MeV)	$\log_{10} T_{1/2}$ (sec)	
			CPPM	UDL
$^4\text{He}$	$^{203}\text{Ra}$	7.79	-0.7532	-1.2335
$^8\text{Be}$	$^{199}\text{Rn}$	15.43	19.5073	20.1441
$^{12}\text{C}$	$^{195}\text{Po}$	29.92	19.6919	20.1377
$^{13}\text{C}$	$^{194}\text{Po}$	26.73	28.5585	29.6432
$^{16}\text{O}$	$^{191}\text{Pb}$	43.84	23.4615	22.7266
$^{30}\text{Si}$	$^{177}\text{Os}$	85.23	32.4486	26.6377

**Table 4:** Cluster decay half-lives of  $^{208}\text{Th}$  isotope

Cluster	Daughter	Q (MeV)	$\log_{10} T_{1/2}$ (sec)	
			CPPM	UDL
$^4\text{He}$	$^{204}\text{Ra}$	8.09	-1.3628	-1.8297
$^8\text{Be}$	$^{200}\text{Rn}$	15.35	19.738	20.3846
$^{12}\text{C}$	$^{196}\text{Po}$	29.72	20.0869	20.5398
$^{16}\text{O}$	$^{192}\text{Pb}$	44.12	22.811	22.1442

### Conclusions:

We have investigated the alpha decay chains of recently synthesized  $^{207,208}\text{Th}$  isotopes. Various possible cluster emissions from these isotopes with decay half-lives within the experimental upper limit are also predicted.

### References:

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