

## $\Lambda\Lambda$ Hypernuclei and H dibaryon: A Theoretical Search

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### Introduction

The data on strangeness  $S = -2$  hypernuclear system is very less, and no data exist for systems with higher strangeness content. The study of double  $-\Lambda$  hypernuclei could provide valuable information on  $\Lambda\Lambda$  interaction. Experimentally, double hypernuclei can be produced by separated  $K^-$  meson beam accelerator at Brookhaven National Laboratory (BNL), Japanese high energy accelerator research organization (KEK) and European Center for High Energy Physics (CERN). A high statistics measurement of double hypernuclear production has been made using high intensity AGS D6  $K^-$  beam line [1]. The double hypernuclei can be produced via the double strangeness exchange reaction ( $K^-, K^+$ ) by both direct production or by  $\Xi^-$  capture at rest by an emulsion atom. In later reaction meson beam is used to tag the production of  $\Xi^-$  hyperon, which is then slowed down in emulsion and captured at rest by an emulsion atom. In the following sections we discuss the theoretical frontiers of double- $\Lambda$  hypernuclei.

### The s-shell ${}_{\Lambda\Lambda}^4\text{H}$ , ${}_{\Lambda\Lambda}^5\text{H}$ , ${}_{\Lambda\Lambda}^5\text{He}$ and ${}_{\Lambda\Lambda}^6\text{He}$ Hypernuclei

The theoretical study of double- $\Lambda$  hypernuclei started soon after the discovery. Among the well established double- $\Lambda$  hypernuclei, the  ${}_{\Lambda\Lambda}^6\text{He}$  hypernucleus is best studied [2]. The knowledge of  $\Lambda\Lambda$  interaction was too poor, the earliest theoretical efforts on  ${}_{\Lambda\Lambda}^6\text{He}$  are based on a Hartee-Fock mean field calculations, which dates back to 1969. With the advent of Quantum Monte Carlo techniques, the many-body approach aiming to perform microscopic calculations of nuclei and hypernuclei had taken a new turn. The realistic NN and NNN potentials in the non-strange sector to describe nuclear spectra have been evolving for quite a long time. Now, we have

well established Argonne v18 NN potential and Urbana type NNN potential. The information on non-strange sector potentials is inevitably required for hypernuclei made up of nucleons and hyperons. Thus, for such systems, these potentials have to be used in conjunction with NN and  $\Lambda\text{NN}$ ,  $\Lambda\Lambda$  and  $\Lambda\Lambda\text{N}$  potentials.

The earlier calculations however were quite simple based upon central potentials and a wave function involving central correlations. In the simplest approach all the four nucleons of  ${}_{\Lambda\Lambda}^6\text{He}$  are treated as an alpha cluster and calculations have been performed using  $\alpha\Lambda$  nuclear potentials. On the other hand, central  $\Lambda\text{N}$  potentials have been used at a microscopic level. However, as a marked difference this was performed using Nijmegen simulated  $\Lambda\Lambda$  potentials. Undoubtedly, this study is far from being realistic as it involves only central potentials and correlations. An improved VMC study involving a realistic Hamiltonian and operatorial correlations has also appeared but it ignores space-exchange correlation (SEC) in the wave function [3]. It is evident from a recent work that a study ignoring SEC would be deficient and misleading as it significantly affects every physical observable [4]. The SEC effects are expected to be more evident in  ${}_{\Lambda\Lambda}^6\text{He}$  hypernucleus because of the presence of a pair of hyperons. The Faddeev-Yakubovsky calculations have been extended to all the s-shell single- and double- $\Lambda$  hypernuclei. In this approach, several  $\Lambda\Lambda$  potential models have been used to calculate  $\Delta B_{\Lambda\Lambda}({}_{\Lambda\Lambda}^6\text{He})$ ,  $\Delta B_{\Lambda\Lambda}({}_{\Lambda\Lambda}^5\text{He})$  and  $\Delta B_{\Lambda\Lambda}({}_{\Lambda\Lambda}^5\text{H})$ . The  $I=1/2$  ( ${}_{\Lambda\Lambda}^6\text{H} - {}_{\Lambda\Lambda}^6\text{He}$ ) hypernuclei are found to be particle stable for all the potential strengths. Calculations have also been performed on  ${}_{\Lambda\Lambda}^4\text{H}$  in order to explore bound state for it. However, calculations yield a negative result even for the strong  $\Lambda\Lambda$  strengths. In contradiction to it, Nemura found a bound state for  ${}_{\Lambda\Lambda}^4\text{H}$  in their variational research using  $4\times 4$  Hamiltonian. However, various strengths of this Hamiltonian are uncertain specially those falling in the

strangeness  $S = -2$  sector. This subject is open for debate.

### The p-shell ${}_{\Lambda\Lambda}^{10}\text{Be}$ and ${}_{\Lambda\Lambda}^{13}\text{B}$ hypernuclei

Theoretical complexities increase with increasing baryon number. As a consequence, microscopic calculations based on BB and BBB interactions have yet not performed on these two systems. However, some cluster model calculations on  ${}_{\Lambda\Lambda}^{10}\text{Be}$  are available in the literature. The most recent among them is Faddeev-Yakubovsky calculations. Some old VMC calculations also exist, where in this hypernucleus is treated as a system of  $\alpha\alpha\Lambda\Lambda$  (two  $\alpha$ s+two  $\Lambda$ s). There are other p-shell hypernuclear calculations on  $A = 7 - 10$   $\Lambda\Lambda$  hypernuclei. Similar calculations are not available on the other event,  ${}_{\Lambda\Lambda}^{13}\text{B}$ .

### H DIBARYON

The H dibaryon is a six quark state (uuddss) in a single QCD bag and not a deuteron like baryon molecule. It has strangeness -2, spin and isospin singlet, and positive parity. H dibaryons may exist separate entity inside double hypernucleus, or they can exist inside the core of neutron star. The H dibaryon are directly related to the double- $\Lambda$  hypernuclei, because the binding energy of two  $\Lambda$ s is directly related to the lower limit of H dibaryon mass. The first H dibaryon was predicted by Jaffe [5] using MIT bag model bound by attractive color magnetic interaction between the quarks. Using this model Jaffe calculated its mass about 2150 MeV, which is less than the  $\Lambda\Lambda$  threshold (2231 MeV) by 81 MeV. Experimentally, the H dibaryon may be produced via ( $K^-$ ,  $K^+$ ) reaction, heavy ion collision, p- nucleus annihilation reaction etc. However, no clear experimental evidence has been found for existence of H dibaryon till now. Some theoretical models such as nonrelativistic quark cluster model, Skyrme model, QCD sum rule and lattice QCD which are applied to calculate the mass of H dibaryon. Some of them predict the bound states. The fully Variational Monte Carlo study with space-exchange correlations could provide valuable information

about H dibaryon. We are proceeding in this direction.

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### References

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