

## Nature of $K^\pi=0_2^+$ band in $^{162}\text{Er}$

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The level structure in N=88-100 isotopes of  $^{156-168}\text{Er}$  under goes a profound change with N. The  $K^\pi=0_2^+$  band moves from below  $K=2_1$   $\gamma$ -band to above it at N=92 and lies highest at N=98. These isotopes have been studied intensively in regard to the collective nature of the  $K=0_2$  band. Recently, Caprio et al. [1] studied the excited states of  $^{162}\text{Er}$  populated in  $\beta$ -decay, in high statistics coincidences with TRIUMF ISAC facility, and resolved several doublets. The absolute B(E2) strength for excitation of  $0_2$  state was determined precisely, as also for some other

transitions, important to determine the nature of  $K=0_2$  band, were measured.

Earlier [2], we studied the  $\gamma$ -g transitions in the decay of  $^{162}\text{Er}$ , using the algebraic Interacting Boson Model [3], which enables a phenomenological fit to level energy data and possibly, also to some E2 transition rates. The DPPQ model [4] provides a microscopic approach without the need of fitting to data. Here we present the results from our DPPQ model analysis for the  $\gamma$ -g,  $K=0_2$ -g and from  $K, I=4, 4$  state and discuss the nature of  $K=0_2$  band in  $^{162}\text{Er}$ . The previous IBM-1 results are also included.

Table -1 The absolute B(E2) ( $e^2b^2$ ) in  $^{162}\text{Er}$  and other static quantities.

Transition	EX	IBM QQ=22.9, PAIR=11.7	DPPQ X=68.0 F <sub>b</sub> =2.0	DPPQ X=66.5, F <sub>b</sub> = 2.0
$0_g \rightarrow 2_g$	4.50 7	4.95	5.16	4.70
$\rightarrow 2_\gamma$	0.104 8	0.118	0.117	0.112
$\rightarrow 2_\beta$	0.042 10	0.0065	0.093	0.100
$0_2 \rightarrow 2_g$		0.0080	0.09	0.137
$\rightarrow 2_\gamma$		0.065	0.46	0.59
Q(2 <sub>1</sub> )		-2.01	-2.05	-1.95
$\beta$			0.267	0.267

In DPPQ model we predict the predominant  $K=0$  component in g-band and ( $2_3, 4_3$ ) states and  $K=2$  for  $2_2, 4_2$  and  $6_2$  states. We also obtain predominant  $K=4$  component in the fourth  $I^\pi=4^+$  state. Caprio et al. [1] obtained the B(E2,  $0_g-2_3$ ) strength of 8(2) WU ( $\sim 0.042 e^2b^2$ ), supporting the collective  $\beta$ -vibration. It is well known that IBM-1 predicts a low  $\beta$ -excitation strength generally, as also obtained by us here (Table-1). Using the  $E_\gamma, I_\gamma$  values from Ref. [5], we deduced the B(E2) ratios in Table 2, 3. The nndc data includes the updated NDS of (2007). However, some values of Ref. [1] are not included by the evaluator. These are marked here (Table 3) by asterisk

The B(E2,  $0_g-2_g$ ) and B(E2,  $0_g-2_\gamma$ ) are well given in IBM-1 and DPPQM (Table 1).

The excitation strength of  $2_\beta$  exceeds the experimental value, signifying larger  $\beta$ -g mixing in DPPQM. The  $2_2-4_1$  E2 transition is very weak in DPPQ calculation and is very sensitive to slight parameterization. In RTR model, B(E2,  $2_\gamma-4_g$ ) is zero for  $\gamma=0^\circ$  and  $30^\circ$  and is 0.020 at  $10^\circ$ . There is large deviation for B(E2) ratios involving such weak transitions, from theory. To illustrate this, two sets of DPPQM value are cited here (Tables 1-3). Other  $\gamma$ -g B(E2) ratios are reproduced in IBM-1 and DPPQM. For E2 transitions from  $2_3=2_\beta$  (Table 3) there is agreement with EX, except for  $2_3-2_2/3$ .

For the  $K=4, I=4$  state the B(E2,  $4-3/2_2$ ) agrees with experiment in both models. But for  $4_2/2_2$  ratio DPPQ value is larger

Table 2. B(E2) ratios for  $\gamma$ -g in  $^{162}\text{Er}$ .

Transition	EX	Alaga	IBM [2]	DPPQ -1	DPPQ -2	RVM [1]
$2_2 \rightarrow 0/2$	0.42 2	0.70	0.65	0.31	0.235	
$\rightarrow 4/2$	0.12 8	0.05	0.064	0.016-E03	0.0045	
$3 \rightarrow 2/4$	0.71 9	2.50	2.03	1.46	1.32	1.01
$4_2 \rightarrow 2/4$	0.077 20	0.34	0.29	0.075	0.060	0.05
$\rightarrow 6/4$	1.29 20	0.09	0.13	0.0017	0.0022	0.055
$\rightarrow 2_2/4$	10*		11.5	7.0	6.0	
$5 \rightarrow 4/6$	0.58 6	1.75	1.26	0.85	0.75	0.47
$\rightarrow 4/4_2$	0.0014		0.044	0.055	0.066	
$6_2 \rightarrow 4/6$	0.11 2	0.27	0.216	0.028	0.21	
$\rightarrow 6/4_2$	0.036 5		0.044	0.068	0.081	
$\rightarrow 4_2/5$	0.19 5		1.7	2.30	2.28	

\* $4_2 \rightarrow 2_2 I_\gamma$  is not listed in [5]. If a relative intensity of 1 is assumed, it yields the ratio=10 in agreement with theory.

Table 3. B(E2) ratios for  $\beta$ -g in  $^{162}\text{Er}$ .

Transition	EX	[1] W.u	IBM [2]	DPPQ -1	DPPQ-2
$2_3 \rightarrow 0$	0.008	1.6 3	0.0013	0.019	0.020
$\rightarrow 2$	0.0012	2.5 5	0.0021	0.0071	0.0057
$\rightarrow 4$	0.0025	4.9	0.0047	0.082	0.090
$\rightarrow 2_2$	0.18	<37	0.0164	0.140	0.18
$\rightarrow 3$	3.3*	<660*	0.032	0.23	0.33
$0_2 \rightarrow 2_g/2_2$	0.007 2		0.12	0.20	0.23
$2_3 \rightarrow 0/2$	0.63 6		0.62	1.58	3.5
$\rightarrow 2_2/2_1$	< 14.3 *		7.8	4.57	31.5
$\rightarrow 4/0$	3.1 2		3.6	4.60	4.50
$\rightarrow 2_2/3$	0.054*		1.96	0.30	0.545
$4_4 \rightarrow 3/2_2$	1.07 11		0.610	1.04	1.21
$\rightarrow 4_2/2_2$	0.26 16		0.24	0.76	1.03

\*Values from [1]. The  $2_3 \rightarrow 3_1 I_\gamma$  assumed in [1] yields too large B(E2) due to large  $E_\gamma^5$  ratio.

### Discussion

The level structure and B(E2) values, as well as  $\gamma$ -g and  $\beta$ -g transitions are well given in IBM-1 and DPPQM. Our study supports the K=0<sub>2</sub> band to be beta band and 4<sub>4</sub> state as predominantly K=4.

### References

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