

## Signature partners pairs in triaxial superdeformed bands of $^{164}\text{Lu}$ isotopes

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### Introduction

A mass region (160) containing  $N \sim 94$  and  $Z \sim 72$  is of special interest in the field of nuclear structure physics. Potential energy surface calculations (PES) confirms the existence of exotic shapes with prolate deformation in the  $A \sim 160$  mass region. Thus, the PES calculations allocates a remarkable probability of investigating superdeformed (SD) shapes with prominent triaxiality. Experimentally, Petersen and Schmitz [1, 2] found such case in  $^{163,165}\text{Lu}$  with a large quadrupole moment values ( $\varepsilon_2 \approx 0.4$ ,  $\gamma \sim +18^\circ$ ). In the  $A \sim 160$  mass region, the triaxiality is associated with the movement of the high-j single quasiparticle outside the SD core. The introduction of the wobbling mode provides the confirmation of triaxiality in the SD spectroscopy. At deformation  $\varepsilon_2 \approx 0.4$  and  $\gamma \sim 20^\circ$ , a gap around  $N=94$  proves to be important for the evolution of triaxial superdeformed shapes (TSD) in the  $A \sim 160$  mass region. The TSD bands and their decayed strength in  $^{164}\text{Lu}$  was studied by Tormanen et al. [3]. Gammasphere spectrometer was used by Bringel et al. [4] to investigate the eight TSD bands in  $^{164}\text{Lu}$ . The band head spin of triaxial SD bands in Lu isotopes was determined by Sharma et al. [5].

In this present paper, we have calculated the band head moment of inertia ( $\mathfrak{S}_0$ ) for triaxial SD bands in  $^{164}\text{Lu}$  isotopes. Here, we have considered only  $^{164}\text{Lu}(1,2,3)$  triaxial SD bands and neglected  $^{164}\text{Lu}(4,5,6,7,8)$  triaxial SD bands as there corresponding band head

spins are not known. To do this work we have employed the nuclear softness formula.

### Formalism

#### Nuclear softness formula

Nuclear softness formula was formalised by Gupta [6]. The energy levels of ground state bands in even-even nuclei have been taken into the account. Identical formulation was given for transitional and well deformed nuclei called as soft rotor formula [7]. The transition energies for the SD bands can be expressed as

$$E_\gamma = \frac{\hbar^2}{2\mathfrak{S}_0} \times \left[ \frac{I(I+1)}{1+\sigma I} - \frac{(I-2)(I-1)}{1+\sigma(I-2)} \right]. \quad (1)$$

where  $\mathfrak{S}_0$  and  $\sigma$  are the model parameter, which can be found by the fitting procedures.

TABLE I: Parameters obtained from least square fitting for triaxial SD bands of  $^{164}\text{Lu}$  isotopes by using Nuclear softness formula.

TSD BANDS	$E_\gamma(I \rightarrow I-2)$	$\mathfrak{S}_0$
$^{164}\text{Lu}(1)$	374	89.7
$^{164}\text{Lu}(2)$	354	89.4
$^{164}\text{Lu}(3)$	536	73.9

### Results and Discussion

Signature partner SD bands are the one which have same values of band head moment of inertia ( $\mathfrak{S}_0$ ). Following this definition we have applied the nuclear softness formula to calculate the band head moment of inertia ( $\mathfrak{S}_0$ ) for triaxial SD bands in  $^{164}\text{Lu}$ . The data has been taken from the tables of SD bands given by Singh et al.[8] and from Ref. [9]. It is noticed from Table I that the obtained band head moment of inertia ( $\mathfrak{S}_0$ ) of triaxial

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SD band in  $^{164}\text{Lu}(1)$  is same as that of triaxial SD band in  $^{164}\text{Lu}(2)$ . Hence, triaxial SD band in  $^{164}\text{Lu}(1)$  and  $^{164}\text{Lu}(2)$  are the signature partner bands.

### Conclusion

In this present work, it is very well noticed that the identical value of band head moment of inertia ( $\mathfrak{S}_0$ ) of triaxial SD bands in  $^{164}\text{Lu}(1)$  and  $^{164}\text{Lu}(2)$  obtained by the nuclear softness formula verified the experimentally observed signature partner bands.

### References

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