# Is there a wobbling band in $^{129}$ Cs?

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# Introduction

Investigations on the negative parity onequasiparticle bands of odd-A triaxial nuclei in the  $A \approx 130$  region have gained new momentum recently, following a re-evaluation of their structure in terms of the *wobbling mode* in certain cases [1,and references therein]. The wobbling motion is considered one of the experimental fingerprints of triaxiality, along with chirality and  $\gamma$ -vibration. In odd-Z nuclei below Z = 64 sub-shell closure,  $^{151}_{63}$ Eu,  $^{139}_{61}$ Pm,  $^{135}_{59}$ Pr, and  $^{133}_{57}$ La are found to exhibit wobbling motion. However, no such bands have been reported in any of the 55Cs isotopes, although the observation of several chiral bands in these isotopes indicates their triaxial shapes. The experimental identification of this phenomenon depends on the E2 and M1 amplitudes of the  $\Delta I = 1 \gamma$ -transitions between successive phonon wobbling bands [2]. In this context, determination of the multipole mixing ratio ( $\delta$ ) of the connecting transitions between the so-called *signature partner* bands becomes crucial.

A recent study has shown that the existence of a wobbling mode in odd-A nuclei depends on the deformation of their *even-even* neighboring nuclei [3]. Based on this, the <sup>129</sup>Cs has been identified as a potential candidate for exhibiting wobbling motion. The currently available spectroscopic results provide intriguing insights into this matter [4]. Therefore, in this work, the angular correlation  $(R_{DCO})$  and linear polarization (P) measurements were carried out for the  $\Delta I = 1$  transitions of interest to determine the mixing ratio of these transitions.

# **Experimental Details**

Excited states of <sup>129</sup>Cs were populated via the  $^{127}$ I(<sup>4</sup>He,  $2n\gamma$ ) reaction at  $E_{\alpha} = 33$  MeV, utilising the K-130 cyclotron at VECC, Kolkata. The target consisted of elemental iodine beads, sandwiched between Kapton tapes. Indian National Gamma Array [5], with eleven Compton-suppressed HPGe Clover detectors and a planer HPGe LEPS, served as the  $\gamma$ -spectrometer. A PIXIE-16 digital data acquisition system recorded  $\gamma$  events in both single and coincidence modes [6]. Offline data were sorted and analysed with BiNDAS [7], INGASORT [8], and RADWARE [9] codes.

## Results

FIG. 1 shows the low-spin part of the  $\pi h_{11/2}$ band of <sup>129</sup>Cs. From the earlier reported angular distribution coefficients,  $\delta \approx -0.3$  or  $\delta \approx -2.2$  were



FIG. 1: Negative parity states of interest in <sup>129</sup>Cs.

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FIG. 2: Left: Contour plot of the calculated angular distribution coefficients  $(a_2, a_4)$  for different values of  $\delta$ (black). Corresponding dispersion of the experimental data is marked with blue cross. Right: The  $\chi^2$  analysis for experimental  $a_2$  and  $a_4$  of the 668 keV  $\gamma$ -ray.

estimated for the 668 keV transition [4]. However, the  $\chi^2$  analysis indicates a comparatively higher probability for the lower value of  $\delta$ , as presented in FIG. 2. In the present spectroscopic study, the  $R_{DCO}$  and P of the 668 keV transition have been measured. The value of  $R_{DCO}$  is influenced by the initial spin alignment of the residual nucleus emitting the  $\gamma$ -ray, represented by the width of the substate population  $(\sigma/J)$ , and by the mixing ratio  $(\delta)$ in the case of a mixed transition. In  $\alpha$ -induced reactions, like those in this study, the  $\sigma/J$  value is expected to be broader ( $\sigma/J = 0.37(3)$  [12]) compared to heavy-ion induced reactions, where typically  $\sigma/J \approx 0.3$ . For the present nuclear reaction, the value of  $\sigma/J = 0.36(2)$  was estimated by comparing the experimental  $R_{DCO}$  of the 182 keV  $\gamma$ -ray with its calculated values (FIG. 3). Using this, the  $R_{DCO}$  and P of the 668 keV  $\gamma$ -ray were calculated for different values of  $\delta$ . By comparing these calculated  $R_{DCO}$  and P values with their experimentally measured values,  $\delta = -3.5(2)$  was estimated



FIG. 3: Plot of the calculated (black) and measured (red / magenta) R<sub>DCO</sub> values of 182 keV  $\gamma$ -ray (7/2<sup>+</sup>  $\rightarrow$  $5/2^+, \delta = 0.25(2)$  [10, 11]), as a function of  $\sigma/J$ .



FIG. 4: Left: Contour plot of the calculated R<sub>DCO</sub> and P for different values of  $\delta$  (black). Corresponding dispersion of the experimental data is marked with blue cross. Right: The  $\chi^2$  analysis of experimental R<sub>DCO</sub> and *P* for the 668 keV  $\gamma$ -ray.

for this transition (FIG. 4), indicating a large E2contribution. Therefore, the band above the  $13/2^{-1}$ state in <sup>129</sup>Cs most likely originates from the excitation of a wobbling phonon.

#### Summary

In summary, excited states in  $^{129}\mathrm{Cs}$  were populated through  $\alpha$ -induced reactions with a <sup>127</sup>I target at a beam energy of 33 MeV. The present spectroscopic results show a large E2 admixture in the 668 keV  $\gamma$ -ray, indicating the existence of a wobbling mode in this nucleus. Further data analysis is underway and will be presented at the symposium.

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